

Fixed Point Binary

In denary we represent number, or parts of numbers, that are less than one like this:

100	10	1	.	1/10	1/100	1/1000
3	6	9	.	7	5	2

In binary, we use the same tactic:

8	4	2	1	.	1/2	1/4	1/8	1/16
1	0	1	0	.	1	1	0	0
			10	.	75	(10)		

Converting fixed point binary to denary

Convert the integer part as normal, then add the fractions together:

$0.1_{(2)}$	=	$\frac{1}{2}$	=	$0.5_{(10)}$
$0.01_{(2)}$	=	$\frac{1}{4}$	=	$0.25_{(10)}$
$0.001_{(2)}$	=	$\frac{1}{8}$	=	$0.125_{(10)}$
$0.0001_{(2)}$	=	$\frac{1}{16}$	=	$0.0625_{(10)}$

Converting denary to fixed point binary

Convert the integer part as normal, then remove the fractions:

E.G. 11.6875 [= 1010.1011]

Integer part = $1010_{(2)}$

Remove 0.5 from the fractional part = $1010.1_{(2)}$

Remaining: $0.1875_{(10)}$

Can't remove 0.25 from the fractional part = $1010.10_{(2)}$

Remaining: $0.1875_{(10)}$

Remove 0.125 from the fractional part = $1010.101_{(2)}$

Remaining: $0.0625_{(10)}$

Remove 0.0625 from the fractional part = $1010.1011_{(2)}$

Remaining: $0_{(10)}$

Binary Multiplication

Binary multiplication uses the following rules (obvious when you think about it):

$$0 \times 0 = 0$$

$$0 \times 1 = 0$$

$$1 \times 0 = 0$$

$$1 \times 1 = 1$$

E.G. 1 – 1100×0010 [= 11000]

$$\begin{array}{r}
 1100 \\
 \underline{0010} \times \\
 \\
 \text{Multiply by the right hand number:} \quad 0000 \\
 \text{Multiply by the next number:} \quad 1100 \\
 \text{Multiply by the next number:} \quad 0000 \\
 \text{Multiply by the next number:} \quad \underline{0000} \\
 \\
 11000
 \end{array}$$

We can effectively ignore any 0s in the bottom number.

E.G 2 – 00101010×00010010 [= 110100100]

$$\begin{array}{r}
 00101010 \\
 \underline{00010010} \times \\
 \\
 00101010 \\
 \underline{00101010} \quad + \\
 \\
 110100100
 \end{array}$$